

# Strong Coupling Constant from the Photon Structure Function

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## Abstract

We extract the value of the strong coupling constant  $\alpha_s$  from a single-parameter pointlike fit to the photon structure function  $F_2^\gamma$  at large  $x$  and  $Q^2$  and from a first five-parameter full (pointlike and hadronic) fit to the complete  $F_2^\gamma$  data set taken at PETRA, TRISTAN, and LEP. In next-to-leading order and the  $\overline{\text{MS}}$  renormalization and factorization schemes, we obtain  $\alpha_s(m_Z) = 0.1183 \pm 0.0050(\text{exp.})_{-0.0028}^{+0.0029}(\text{theor.})$  [pointlike] and  $\alpha_s(m_Z) = 0.1198 \pm 0.0028(\text{exp.})_{-0.0046}^{+0.0034}(\text{theor.})$  [pointlike and hadronic]. We demonstrate that the data taken at LEP have reduced the experimental error by about a factor of two, so that a competitive determination of  $\alpha_s$  from  $F_2^\gamma$  is now possible.

The theory of strong interactions, Quantum Chromodynamics (QCD), is one of the corner stones of the Standard Model of elementary particle physics. The precise determination of its fundamental parameter, the strong coupling constant  $\alpha_s$ , bears important implications for the validity not only of QCD itself, but also of even more fundamental theories, since these have to contain the Standard Model as an effective field theory in the low-energy limit. A more fundamental theory, which might explain the size of the strong coupling constant, has yet to be established. Therefore,  $\alpha_s$  must currently be extracted from experiment. Among the large variety of processes that have been used to this end, the most precise values have been obtained in  $Z$ -boson- and  $\tau$ -decays at LEP, scaling violations in structure functions at HERA, and quarkonium decay branching fractions and lattice calculations of quarkonium mass splittings, leading – together with other, less precise measurements – to a current world average of  $\alpha_s(m_Z) = 0.1172 \pm 0.0020$  at the mass of the  $Z$ -boson,  $m_Z = 91.1876$  GeV [1].

When the photon structure function  $F_2^\gamma$  was first discussed in the context of QCD, a precise determination of  $\alpha_s$  quickly emerged as one of its most interesting applications. Due to the pointlike coupling of the photon to quarks, the leading order (LO,  $\mathcal{O}(\alpha_s^{-1})$ ) [2] and next-to-leading order (NLO) [3] contributions to  $F_2^\gamma(x, Q^2)$  are calculable in QCD perturbation theory, if the virtuality  $Q$  in the deep-inelastic electron-photon scattering process is significantly larger than the asymptotic scale parameter  $\Lambda$ . Unfortunately, this pointlike contribution exhibits a power singularity at small Bjorken- $x$  [4], which becomes rapidly stronger in higher orders [5]. The singularity can be regularized with a non-perturbative [6] or transverse-momentum [7] cut-off, but then the sensitivity to  $\alpha_s$  is reduced and a dependence on the unphysical cut-off is introduced [8]. It is then necessary to fit both  $\alpha_s$  and the cut-off to experimental data. Alternatively, the singularity can be canceled order by order in perturbation theory by retaining a hadronic boundary condition at a low starting scale  $Q_0$  [9, 10]. In this case it is necessary to fit  $\alpha_s$  and the hadronic input to experimental data. However, the evolution of the hadronic input to the physical scale  $Q$  is still predicted by perturbative QCD through inhomogeneous evolution equations [11], and the negligibility of the hadronic input can be tested *a posteriori*. Both methods have been applied in the past to PEP and PETRA data yielding  $\Lambda_{\overline{\text{MS}}}^{(4)} = 180_{-90}^{+100}$  MeV [12] or  $\alpha_s(m_Z) = 0.108_{-0.010}^{+0.008}$ . This value contributed to the world average in the 1988 [13], 1990 [14], and 1992 [15] issues of the Review of Particle Properties, but was then abandoned on the grounds that there were “no new results and the data do not contribute significantly to the average” [16]. Since then it

has been widely believed [17, 18, 19, 20, 21] that the sensitivity of  $F_2^\gamma$  to  $\alpha_s$  is small.

In this Letter, we wish to point out that over the last decade a wealth of new  $F_2^\gamma$  data has been collected at the  $e^+e^-$ -colliders TRISTAN and LEP, which extends to high average values of  $Q^2$ ,  $\langle Q^2 \rangle \leq 780 \text{ GeV}^2$ . We demonstrate that the new data improve the sensitivity of  $F_2^\gamma$  to  $\alpha_s$  significantly and that a single-parameter pointlike fit as well as a five-parameter full (pointlike and hadronic) fit to PETRA, TRISTAN, and LEP data yield results, which are not only consistent with the world average, but also have competitive experimental and theoretical errors.

We work in a fixed flavor number scheme with three active quark flavors ( $u, d, s$ ). It is well known [22] that for current measurements of  $F_2^\gamma$  the available hadronic energy squared  $W^2 = Q^2(1-x)/x$  is not much larger than the production threshold  $4m_h^2$  of the heavy quarks ( $h = c, b, t$ ), so that mass effects can not be neglected and the massive, fixed order  $\mathcal{O}(\alpha)$  expression for the Bethe-Heitler process  $\gamma^*(Q^2)\gamma \rightarrow h\bar{h}$  [23] should be used instead of the massless, factorized  $\mathcal{O}(\alpha/\alpha_s)$  expression. For a consistent NLO analysis, we do not include the known [24], but numerically small,  $\mathcal{O}(\alpha\alpha_s)$  corrections to the Bethe-Heitler process and omit the  $\mathcal{O}(\alpha\alpha_s^2)$  contributions from the process  $\gamma^*(Q^2)g \rightarrow h\bar{h}$ . The heavy quark masses are not well constrained from measurements of  $F_2^\gamma$ . We adopt a charm quark mass of  $m_c = 1.5 \pm 0.1 \text{ GeV}$  in good agreement with recent precise determinations from threshold production at  $e^+e^-$ -colliders [25]. At large  $Q^2$ , charm quarks contribute up to 40 % to  $F_2^\gamma$  in the whole  $x$ -range, while at small  $Q^2$  they contribute at most 10% below  $x \sim 0.2$ . The contribution from bottom quarks is suppressed by a relative factor 1/16 from the different quark charges, while the threshold for top quark production lies at extremely small  $x = 10^{-5} \dots 10^{-3}$ , so that these contributions are both numerically negligible.

Since we wish to omit spurious higher order terms, which arise from the convolution of NLO contributions to the parton densities with the NLO Wilson coefficients and lead to instabilities at large  $x$  [22], we choose to work in Mellin moment space, where the convolutions reduce to simple products, the evolution can be done analytically and without any approximations, and spurious higher order terms can be consistently omitted. The resulting prediction for  $F_2^\gamma$  is then converted back to  $x$ -space using a numerically fast inverse Mellin transform [26] and fitted to experimental measurements with the multidimensional minimization algorithm MINUIT [27]. The quality of the fit is measured in terms of the  $\chi^2$  value per degree of freedom,  $\chi^2/\text{DF}$ , for all selected data points.

We include in our analysis all published measurements of  $F_2^\gamma$  collected at the high-energy  $e^+e^-$ -colliders PETRA [28, 29, 30, 31], TRISTAN [32, 33, 34], and LEP [35, 36, 37, 38, 39, 40, 41, 42, 43]. If more than one set of statistically overlapping data exists, the most recent publication is used. We exclude from our fit the data published by the TPC/Two-Gamma Collaboration at PEP [44, 45], since several data points, mainly at low  $x$ , are inconsistent with measurements published by PLUTO [29], L3 [37], and OPAL [42] in the range  $1.9 < Q^2 < 5.1 \text{ GeV}^2$ . Data where the charm component has been subtracted are also discarded. The statistical uncertainties and the correlations between data points due to the experimental unfolding are taken into account as provided by the experiments, while the systematic uncertainties are assumed to be uncorrelated. Due to this assumption the values of  $\chi^2/\text{DF}$  are expected to be on average slightly less than unity. If asymmetric errors are given by the experiments, the data points are taken at the center of the full error interval. Most experiments have not corrected for the finite virtuality of the target photon  $P^2$ . We neglect  $P^2$  in this analysis, since usually  $P^2 \ll Q^2$ .

For our pointlike fit, we identify the starting scale  $Q_0$  with the asymptotic scale parameter  $\Lambda$ , so that the hadronic input vanishes automatically and only a single parameter ( $\Lambda$ , or equivalently  $\alpha_s(m_Z)$ ) has to be fitted. As discussed above, this is only justified at large  $x$  and  $Q^2$ , where the residue of the pointlike singularity is expected to be small. Therefore, we perform our single-parameter pointlike fit only to a subset of data points with  $x \geq 0.45$  and  $Q^2 \geq 59 \text{ GeV}^2$ . Very similar results are obtained with the widely used values of  $Q_0 = 0.5 \dots 0.6 \text{ GeV}$  [17, 18, 19, 21], while choosing  $Q_0 = 1 \text{ GeV}$  significantly increases the value of  $\chi^2/\text{DF}$ ; two-parameter pointlike fits of  $\alpha_s$  and  $Q_0$  are driven to  $Q_0 \simeq \Lambda$ . In the first three lines of Tab. I we list the  $\chi^2/\text{DF}$  and  $\alpha_s(m_Z)$  values obtained in LO and NLO. The NLO fit is performed in two factorization schemes ( $\overline{\text{MS}}$  and  $\text{DIS}_\gamma$  [22]) with different treatment of the pointlike Wilson coefficient in  $F_2^\gamma$ , but the numerical variation is found to be small. The total values of  $\chi^2/\text{DF}$  as well as those for the individual data sets (not shown) lie around unity or below, indicating that the pointlike photon structure function and the fitted values of  $\alpha_s(m_Z)$  describe the data sets well within their statistical and systematic uncertainties. The experimental errors are determined by varying  $\alpha_s(m_Z)$  until the total value of  $\chi^2$  is increased by one unit. To estimate the theoretical error, we vary the charm quark mass as indicated above and follow the common convention of varying the factorization and renormalization scales by factors of two about their central value, the physical scale  $Q$ . We then add these

TABLE I:  $\chi^2/\text{DF}$  and  $\alpha_s(m_Z)$  values obtained in LO and NLO in the  $\overline{\text{MS}}$  and  $\text{DIS}_\gamma$  factorization schemes with a single-parameter fit of the pointlike photon structure function  $F_2^\gamma$ . Also shown are the results obtained without LEP data and with very high  $Q^2$  data.

Order	Scheme	Experimental Data	$Q_0/\text{GeV}$	$\chi^2/\text{DF}$	$\alpha_s(m_Z)$
LO	–	$Q^2 \geq 59 \text{ GeV}^2, x \geq 0.45$	$\Lambda_{\text{LO}}^{(3)}$	7.9/ 19	$0.1260 \pm 0.0055(\text{exp.})_{-0.0055}^{+0.0061}(\text{theor.})$
NLO	$\overline{\text{MS}}$	$Q^2 \geq 59 \text{ GeV}^2, x \geq 0.45$	$\Lambda_{\overline{\text{MS}}}^{(3)}$	9.1/ 19	$0.1183 \pm 0.0050(\text{exp.})_{-0.0028}^{+0.0029}(\text{theor.})$
NLO	$\text{DIS}_\gamma$	$Q^2 \geq 59 \text{ GeV}^2, x \geq 0.45$	$\Lambda_{\overline{\text{MS}}}^{(3)}$	8.1/ 19	$0.1195 \pm 0.0051(\text{exp.})_{-0.0032}^{+0.0031}(\text{theor.})$
NLO	$\text{DIS}_\gamma$	$Q^2 \geq 59 \text{ GeV}^2, \text{ w/o LEP}$	$\Lambda_{\overline{\text{MS}}}^{(3)}$	3.2/ 7	$0.1244 \pm 0.0126(\text{exp.})_{-0.0032}^{+0.0033}(\text{theor.})$
NLO	$\text{DIS}_\gamma$	$Q^2 \geq 284 \text{ GeV}^2, \text{ all } x$	$\Lambda_{\overline{\text{MS}}}^{(3)}$	11.9/ 8	$0.1159 \pm 0.0125(\text{exp.})_{-0.0018}^{+0.0018}(\text{theor.})$

three individual errors in quadrature. The LO value of  $\alpha_s(m_Z)$  is consistent with the NLO value within the expected accuracy,  $\mathcal{O}(\alpha_s^2)$ , and the theoretical error is reduced from LO to NLO as expected. In the fourth line of Tab. I, we list the result of a fit without the LEP data. The experimental error is more than doubled, showing that the LEP data have considerably increased the sensitivity of  $F_2^\gamma$  to  $\alpha_s$  at high  $x$  and  $Q^2$ . When data at all values of  $x$ , but very high  $Q^2$  ( $Q^2 \geq 284 \text{ GeV}^2$ ) are fitted, the central value of  $\alpha_s(m_Z)$  remains virtually unchanged (last line of Tab. I). At very high  $Q^2$ , the theoretical error drops by a factor of two, whereas the experimental error increases. Measurements of  $F_2^\gamma$  at a future linear  $e^+e^-$ - or  $e\gamma$ -collider like TESLA at very high values of  $Q^2$  and with small experimental errors will therefore lead to even more precise determinations of  $\alpha_s$ .

The goodness of our pointlike fit may also be judged from Fig. 1, where the fitted data points are shown as full circles, while those that have been omitted from the fit are shown as open circles, and where the statistical and systematic errors have been added in quadrature. The theoretical curves are perturbatively stable, *i.e.* LO and NLO fits differ only by small amounts. The choice of factorization scheme clearly affects the region of very large  $x$ , but it has only a minor effect on the description of the data. Also shown in Fig. 1 is the hadronic contribution from a five-parameter NLO fit of the full (pointlike and hadronic) photon structure function in the  $\text{DIS}_\gamma$  scheme. It clearly falls from small to large  $x$  and  $Q^2$  and amounts to only a few percent in the region that has been used in the pointlike fit.

For our full (pointlike and hadronic) fit, we start from the observations that  $F_2^\gamma$  is dominated by the  $u$ -quark density in the photon and is only sensitive to the combined density

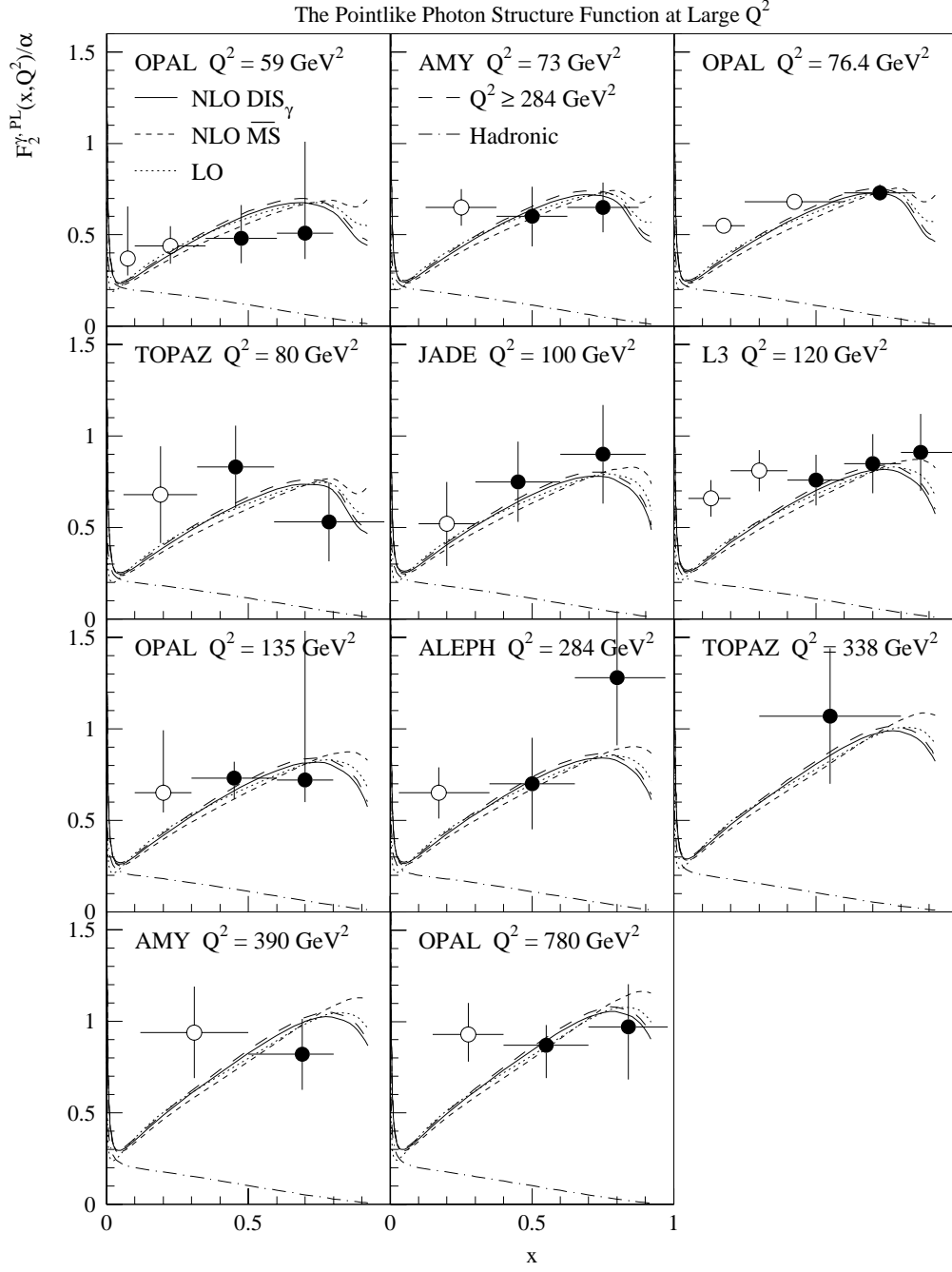


FIG. 1: Single-parameter fits of the pointlike photon structure function, compared to data from PETRA [28], TRISTAN [32, 34], and LEP [35, 39, 40, 41, 43] at large  $Q^2$ . The small- $x$  data points marked by open circles have not been used in the fits. Also shown is the hadronic contribution from a five-parameter NLO fit of the full photon structure function in the  $DIS_\gamma$  scheme.

TABLE II:  $Q_0$ ,  $\chi^2/\text{DF}$ , and  $\alpha_s(m_Z)$  values obtained in LO and NLO in the  $\overline{\text{MS}}$  and  $\text{DIS}_\gamma$  factorization schemes with a five-parameter fit of the hadronic photon structure function  $F_2^\gamma$ . Also shown are the results obtained without data from LEP.

Order	Scheme	Experimental Data	$Q_0/\text{GeV}$	$\chi^2/\text{DF}$	$\alpha_s(m_Z)$
LO	–	all $Q^2$ , all $x$	$0.79 \pm 0.18$	120.9/129	$0.1475 \pm 0.0074(\text{exp.})^{+0.0141}_{-0.0072}(\text{theor.})$
NLO	$\overline{\text{MS}}$	all $Q^2$ , all $x$	$0.83 \pm 0.09$	117.9/129	$0.1198 \pm 0.0028(\text{exp.})^{+0.0034}_{-0.0046}(\text{theor.})$
NLO	$\text{DIS}_\gamma$	all $Q^2$ , all $x$	$0.85 \pm 0.09$	114.6/129	$0.1216 \pm 0.0028(\text{exp.})^{+0.0033}_{-0.0050}(\text{theor.})$
NLO	$\text{DIS}_\gamma$	all $Q^2$ , w/o LEP	$0.46 \pm 0.10$	37.1/ 38	$0.1147 \pm 0.0047(\text{exp.})^{+0.0282}_{-0.0033}(\text{theor.})$

of  $d$ - and  $s$ -quarks, whose contribution is furthermore suppressed by the smaller  $d$ - and  $s$ -quark charges. In addition, the gluon contributes to  $F_2^\gamma$  in LO only through a rather weak coupling to the quark singlet density in the evolution equations. A consecutive fit of the  $u$ -quark,  $d$ - and  $s$ -quark, and gluon densities shows, that only the first is well constrained by  $F_2^\gamma$  data and that the fit does not improve, when more degrees of freedom are added. Therefore we do not impose a hadronic boundary condition for the gluon and assume, that the hadronic fluctuations of the photon are insensitive to the quark charge, *i.e.* we identify the hadronic boundary conditions for  $u$ -quarks and  $d$ - and  $s$ -quarks at the starting scale  $Q_0$ . Together with  $\alpha_s(m_Z)$  and  $Q_0$ , we then fit the parameters  $N$ ,  $\alpha$ , and  $\beta$  of our ansatz  $f_{u,d+s}^\gamma(x, Q_0^2) = Nx^\alpha(1-x)^\beta$  to the full data set described above. In the first three lines of Tab. II we list the  $Q_0$ ,  $\chi^2/\text{DF}$ , and  $\alpha_s(m_Z)$  values obtained with this five-parameter fit in LO and NLO. The starting scale  $Q_0$  is perturbatively stable and is found to be close to the masses of the light vector mesons  $\rho$ ,  $\omega$ , and  $\phi$  in contrast to earlier claims that the perturbative evolution of  $F_2^\gamma$  sets in only at rather high values of  $Q_0 \sim 2 \text{ GeV}$  [46]. The individual and total values of  $\chi^2/\text{DF}$  lie again around unity or below, so that the fitted full photon structure functions describe the full data set well within the experimental uncertainties. Note that the  $\chi^2$  value for the four TPC/Two-Gamma points at  $Q^2 = 2.8 \text{ GeV}^2$ , which have not been used in the fits, is 18.0 and thus very large. The gluon density, generated with  $f_g^\gamma(x, Q_0^2) = 0$ , turns out to be in good agreement [26] with recent H1 dijet data [47]. The experimental errors on the values of  $Q_0$  and  $\alpha_s(m_Z)$  reflect an increase in  $\chi^2$  by one unit, when all other fit parameters are kept fixed. Due to the larger number of data points in the full fit, the experimental error turns out much smaller than in the pointlike fit. When the

full fit is performed without the LEP data (last line of Tab. II), the experimental error is almost doubled, *i.e.* the impact of the LEP data is again impressive. From LO to NLO, the theoretical error is reduced even more than in the pointlike fit. Similar results as those listed in Tab. II are obtained, when only  $u$ -quarks are assigned a hadronic boundary condition.

In Fig. 2 we compare our results to the fitted  $F_2^\gamma$  data in the region of low  $x$  and  $Q^2$ . This region is clearly dominated by the hadronic contribution and by the impact of the LEP data. A fit without the LEP data results in a rise of  $F_2^\gamma$  at low  $x$ , which is much too steep. The fits are perturbatively stable and the data are described almost equally well in the  $\overline{\text{MS}}$  and  $\text{DIS}_\gamma$  scheme.

Since the total error on  $\alpha_s(m_Z)$  is smaller in the full fit than in the pointlike fit due to the larger number of data points, we adopt as our final result

$$\alpha_s(m_Z) = 0.1198 \pm 0.0054 \quad (1)$$

in NLO and the  $\overline{\text{MS}}$  scheme, where the larger theoretical error has been added to the experimental error in quadrature. While our total error is slightly larger than those obtained in  $Z$ -boson- and  $\tau$ -decays at LEP, it is comparable to the errors obtained in deep-inelastic scattering at HERA and heavy quarkonium decays. This encourages us to combine our result with the current world average of  $0.1172 \pm 0.0020$  [1] to a new world average

$$\alpha_s(m_Z) = 0.1175 \pm 0.0019. \quad (2)$$

In conclusion, we have for the first time fitted the now final PETRA, TRISTAN, and LEP data on the photon structure function  $F_2^\gamma$  in NLO of perturbative QCD. We have extracted the value of the strong coupling constant  $\alpha_s(m_Z)$  with competitive experimental and theoretical errors from a single-parameter pointlike fit to data at large  $x$  and  $Q^2$  and from a five-parameter full (pointlike and hadronic) fit at all  $x$  and  $Q^2$ . Our analysis proves that the available  $F_2^\gamma$  data contribute significantly to a precise determination of  $\alpha_s$  and that future measurements of  $F_2^\gamma$  at linear colliders will have a large impact.

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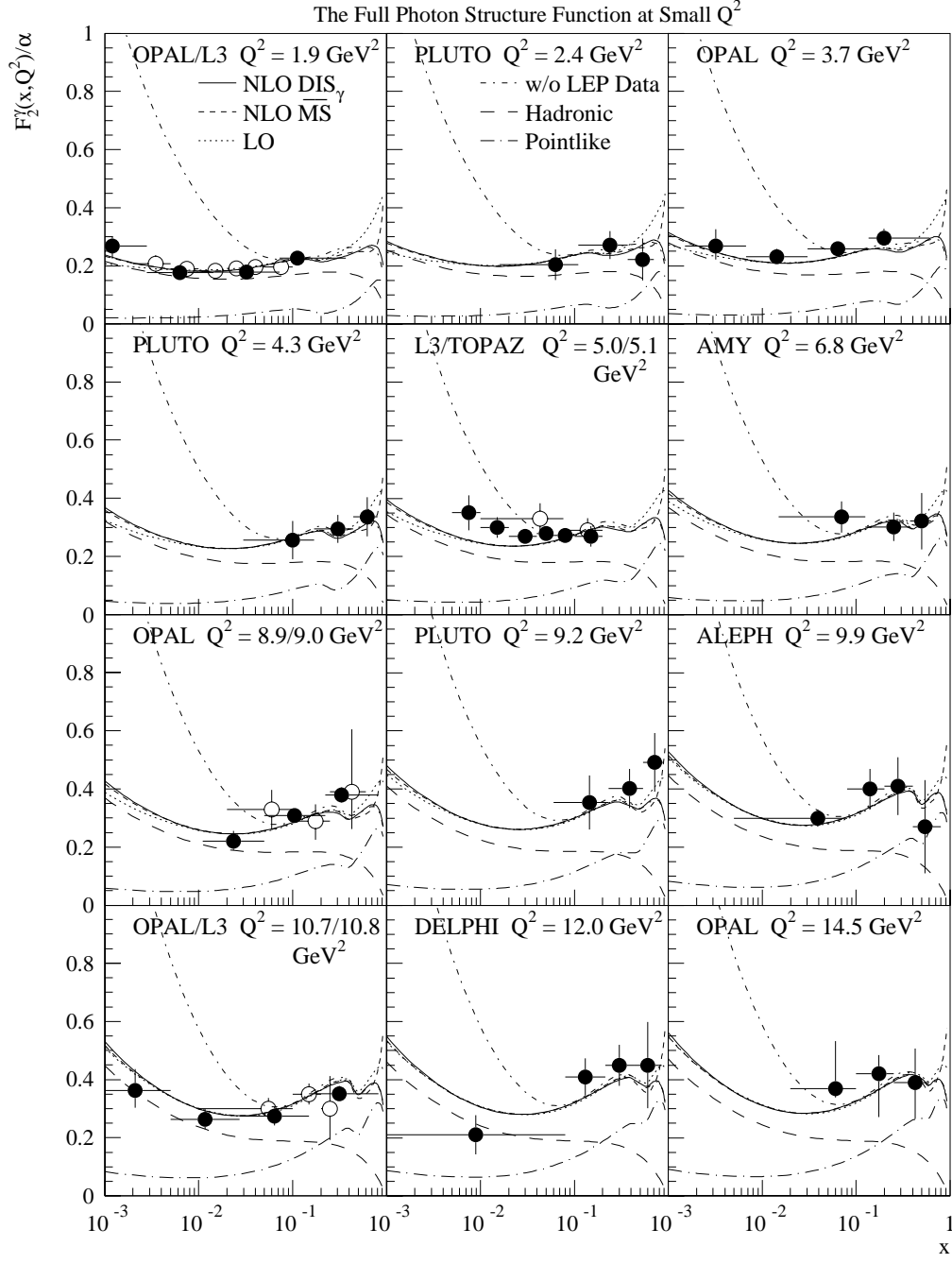


FIG. 2: Five-parameter fits of the full photon structure function, compared to data from PETRA [29], TRISTAN [33, 34], and LEP [35, 36, 37, 38, 40, 42] at small  $Q^2$ . The data points marked by open circles refer to the second experiment and/or  $Q^2$  value. Also shown are the hadronic and pointlike contributions to the NLO fit in the  $\text{DIS}_\gamma$  scheme.

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